

LSB: Local Self-Balancing MCMC in Discrete Spaces

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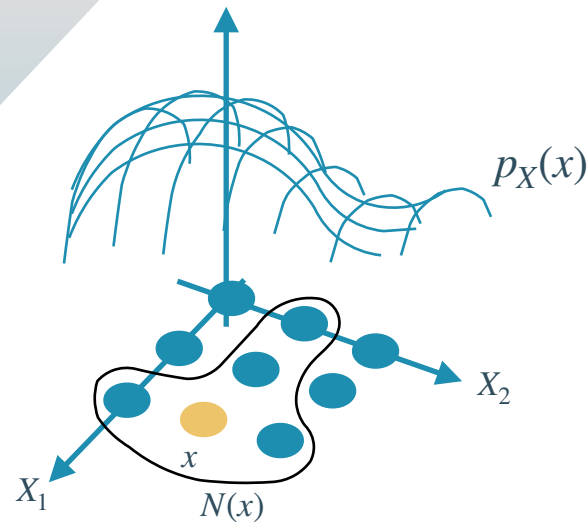
AutoML in
the Wild

Problem

- Sampling in high dimensions $p_X(x) = \frac{\tilde{p}_X(x)}{Z}$
- MCMC $T(x'|x) = A(x',x)Q(x'|x)$
- Locally Balanced Proposal [1]

$$Q(x'|x) = \frac{g\left(\frac{\tilde{p}(x')}{\tilde{p}(x)}\right)1[x' \in N(x)]}{Z(x)}$$

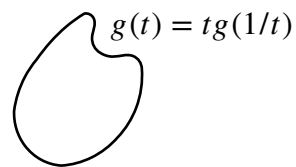
$$g(t) = tg(1/t)$$



Question: How to adapt the proposal . to target . to improve sampling efficiency?

Solution

Parametrizations



Linear (LSB 1)

$$g_\theta(t) = \sum_{i=1}^I \theta_i g_i(t)$$

Nonlinear (LSB 2)

$$g_\theta(t) = \min \left\{ \ell_\theta(t), t \ell_\theta\left(\frac{1}{t}\right) \right\}$$

Any non-negative real function $\ell_\theta(t)$

Objective

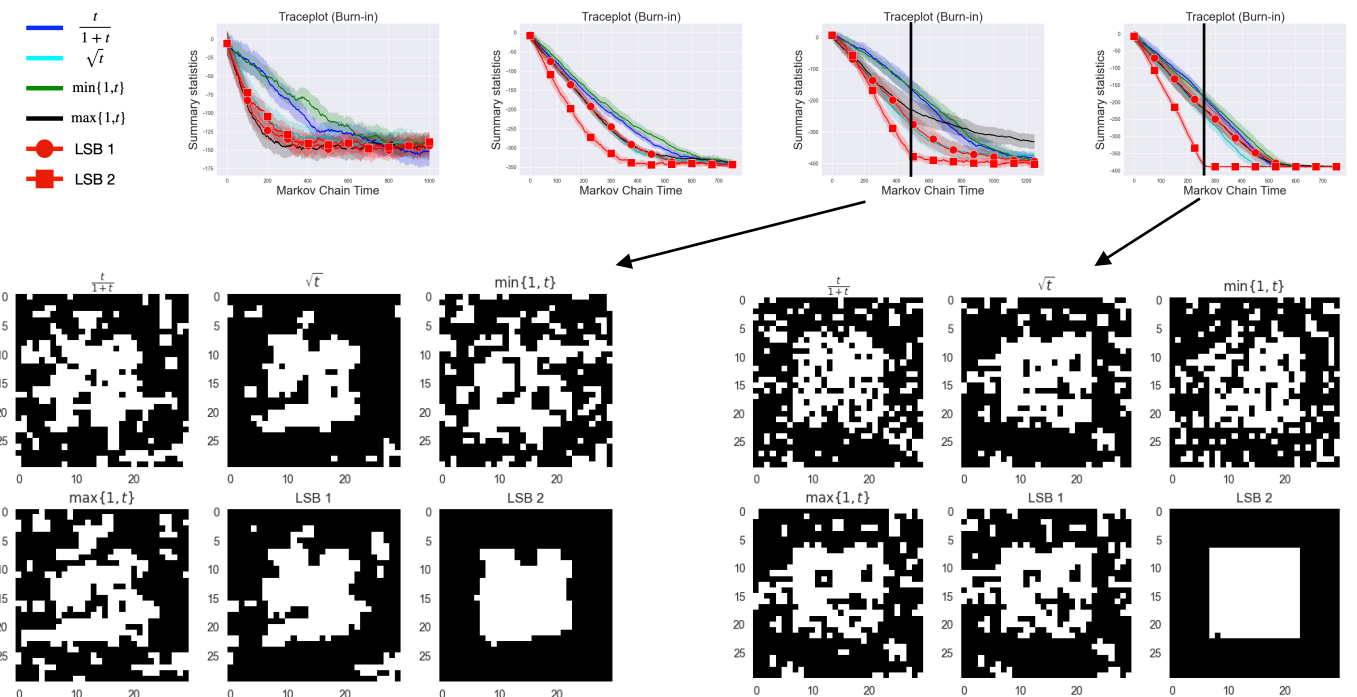
$$I_\theta = KL\{p_X(x)T(x'|x) \| p_X(x)p_X(x')\}$$

Learning procedure

Use historical samples to estimate the objective and update theta at each sampling iteration (during burn-in phase)

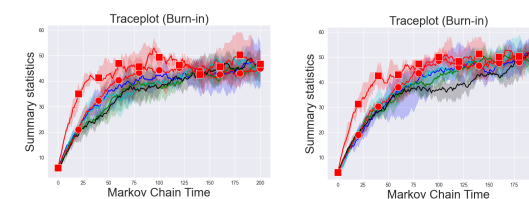
Experiments

2D Ising



Setting	$\frac{t}{1+t}$	\sqrt{t}	$\min\{1, t\}$	$\max\{1, t\}$	LSB 1	LSB 2
Case 1	2.48 ± 0.21	2.30 ± 0.22	2.42 ± 0.19	1.75 ± 0.17	2.50 ± 0.28	2.46 ± 0.28
Case 2	3.33 ± 0.32	2.94 ± 0.36	3.33 ± 0.33	1.72 ± 0.18	2.98 ± 0.24	3.33 ± 0.43
Case 3	2.58 ± 0.73	1.99 ± 0.43	2.56 ± 0.62	1.26 ± 0.12	2.48 ± 0.61	2.67 ± 0.84
Case 4	32.8 ± 9.2	18.5 ± 6.8	31.8 ± 10.0	2.60 ± 1.46	18.4 ± 8.0	30.8 ± 9.2

Bayesian Networks



Dataset	$\frac{t}{1+t}$	\sqrt{t}	$\min\{1, t\}$	$\max\{1, t\}$	LSB 1	LSB 2
BN 1	2.90 ± 0.76	3.41 ± 0.77	2.54 ± 0.32	2.70 ± 0.63	3.19 ± 0.46	3.22 ± 0.38
BN 2	3.43 ± 0.75	3.92 ± 0.94	3.78 ± 0.50	3.63 ± 0.67	3.52 ± 0.42	3.44 ± 0.44

References

[1] Zanella. Informed Proposals for Local MCMC in Discrete Spaces. Journal of the American Statistical Association 2020